

Exemplary Contents with Sample Tasks in Preparation for the Admission Test of the Master Degree Programme Mechatronic and Cyber-Physical Systems

The following collection of sample tasks shall give applicants the opportunity to familiarize themselves with the **exemplary contents** and **level** of the admission test for the Master Programme Mechatronic and Cyber-Physical Systems at the Deggendorf Institute of Technology - study site Campus Cham. Additionally, these tasks represent the range of basic subjects deemed to show elementary, prerequisite knowledge to perform successfully in this master programme. Overall, applicants can obtain a maximum of 90 points within the framework of the aptitude assessment.

Mathematics

A.1 Derivatives

Let $a, x \in \mathbb{R}, a \neq 0$. Calculate the derivative of

$$f(x) = \underbrace{\frac{1}{4a^3\sqrt{2}} \ln\left(\frac{x^2 + ax\sqrt{2} + a^2}{x^2 - ax\sqrt{2} + a^2}\right)}_{=g(x)} + \underbrace{\frac{1}{2a^3\sqrt{2}} \arctan\left(\frac{ax\sqrt{2}}{a^2 - x^2}\right)}_{=h(x)}$$

and simplify as far as possible. Hint: The final expression is surprisingly simple. Approximately, half of the points are for simplifying. Differentiate and simplify $g(x)$ and $h(x)$ separate as far as possible. In means, the natural logarithm.

A.2 Partial Fractions

Expansion into partial fractions.

Let $x \in \mathbb{R}, x^2 \neq 1$. Determine the real coefficients A, B, C, D such that

$$\frac{6x^3 + 2x^2 + 2x - 6}{(x^2 - 1)(x^2 + 1)} = \frac{A}{x-1} + \frac{B}{x+1} + \frac{Cx+D}{x^2+1}.$$

Hint. The answers for A, B, C, D are elements of $\{0, \pm 1, \pm 2, \dots, \pm 9\}$.

A

B

C

D

A.3 Extremum Points

A.4 Integral Calculus

A.5 Matrix, Eigenvalues

Determine to the matrix $A = \begin{pmatrix} 1 & 2 \\ 0,5 & 3 \end{pmatrix}$ the inverse matrix A^{-1} (4P)

Select one:

a. $A^{-1} = \begin{pmatrix} 1 & 0,5 \\ 2 & 3 \end{pmatrix}$

b. $A^{-1} = \begin{pmatrix} 1 & -0,5 \\ -2 & 3 \end{pmatrix}$

c. $A^{-1} = \begin{pmatrix} 1,5 & -1 \\ -0,25 & 0,5 \end{pmatrix}$

d. $A^{-1} = \begin{pmatrix} 1,5 & 0,25 \\ 1 & 0,5 \end{pmatrix}$

e. $A^{-1} = \begin{pmatrix} 1,5 & -0,25 \\ -1 & 0,5 \end{pmatrix}$

Physics

B.1 Velocity

A projectile is launched from level ground with an initial speed v_0 at an angle α with the horizontal. If air resistance is negligible, how long will the projectile remain in the air?

Select one:

a. $\frac{v_0 \sin \alpha}{g}$

b. $\frac{v_0 \cos \alpha}{g}$

c. $\frac{2v_0 \sin \alpha}{g}$

d. $\frac{2v_0}{g}$

e. $\frac{2 \cdot v_0 \cdot \cos \alpha}{g}$

B.2 Distance, Mass, Velocity

A 300-Watt electric wheelchair has a mass of 50 kg, and carries its 50 kg occupant at constant velocity up a long ramp. About how much time does it take the wheelchair to reach the top of the 10-meter high ramp?

Select one:

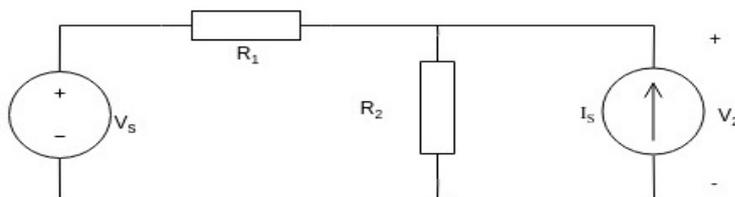
- a. 50 s
- b. 100 s
- c. 33 s
- d. 20 s
- e. 10 s

Electrical Engineering

C.1 Electrical Circuits

Consider the following circuit.

where: $V_s = 12\text{ V}$ $I_s = 4\text{ A}$ $R_1 = 3\ \Omega$ $R_2 = 1\ \Omega$



Find Voltage V_2 .

- Select one:
- a. 4 V
 - b. 2 V
 - c. 4 A
 - d. 6 V
 - e. 8 V

System Theory

D.1 Periodic Time Signals

Which of the signals described below is a periodical time signal?

Select one:

- a. $x(t) = t^2$
- b. $x(t) = a t + b$
- c. $x(t) = a_0 \sin \omega t$
- d. $x(t) = K$

Control Engineering

E.1 Control Loops

A control loop transfer function has the form:

$$F(s) = \frac{1}{s^2/\omega_0 + 2D/\omega_0 s + 1}$$

In which value range of the parameter D (damping) does the transient response of the controlled variable y show no oscillating behaviour?

Select one:

- a. $0 < D < 1$
- b. $D > 1$
- c. $D < 0$

F.1 Model-View Controller

What is the "Model-View-Controller"?

Select one:

- A design pattern.
- It is used to model databases.
- A machine learning technique.
- A programming language.

F.2 Algorithm Calculation

F.3 Binary Trees

F.4 Time Complexity

$n^4 + 100 * n^2 + 2^n$ is

Select one:

- $O(2^n)$
- $O(1)$
- $O(n^4)$
- $O(100)$

F.5 Programming Languages and Expressions

Solution Key for Sample Tasks

A.1

Final answer: $g'(x) = \frac{1}{2} \frac{a^2 - x^2}{a^4 + x^4}$, $h'(x) = \frac{1}{2} \frac{a^2 + x^2}{a^4 + x^4}$, $f'(x) = \frac{1}{a^4 + x^4}$

A.2

A: 1, B: 3, C:2, D: 4

A.5

c)

B.1

c)

B.2

c)

C.1

d)

D.1

c)

E.1

a)

F.1

a)

F.4

a)

Good Luck!

